

# Trigonal B<sub>2</sub>O<sub>3</sub> with Higher Space-Group Symmetry: Results of a Reevaluation

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**Summary.** A new crystal structure refinement based on published X-ray diffraction data [1] of the normal pressure modification of B<sub>2</sub>O<sub>3</sub> (B<sub>2</sub>O<sub>3</sub> form I) shows that the correct space group is (152) P<sub>3</sub>121 instead of (144) P<sub>3</sub>1 within limits of error.

**Keywords.** B<sub>2</sub>O<sub>3</sub> form I; Trigonal diboron trioxide; Space group correction.

## Introduction

At normal pressure, B<sub>2</sub>O<sub>3</sub> has a trigonal structure (form I) characterized by a three-dimensional network of corner-linked BO<sub>3</sub> triangles [1]; at high pressure, an orthorhombic modification (form II) prevails consisting of a framework of linked BO<sub>4</sub> tetrahedra [2]. In the opinion of the authors of Ref. [1] the three earlier publications on the crystal structure of B<sub>2</sub>O<sub>3</sub>–I [3–5], all based on space group P<sub>3</sub>1, have to be considered as obsolete.

The structural data published for B<sub>2</sub>O<sub>3</sub>–I by *Gurr, Montgomery, Knutson*, and *Gorres* [1] are presented in Table 1. Transforming the unit cell according to (010/100/001) followed by an origin shift of (0,0,0.204) leads to positional atom coordinates which fit approximately for a structure description in the higher symmetrical space group (152) P<sub>3</sub>121. To verify this hypothesis, the 130 observed structure amplitude values  $F_{\text{obs}}$  which had been obtained from single-crystal diffractometer measurements [1] were converted to a computer file which was then used for new structure refinements.

## Results and Discussion

Structure refinements were performed both in space group P<sub>3</sub>1 and P<sub>3</sub>121. The atomic coordinates given in Table 1 were used in the starting set for space group P<sub>3</sub>1. The same parameters, but after cell transformation and origin shift, served as the starting set for space group P<sub>3</sub>121. The complex scattering functions for neutral atoms [6], unit weights, and the program SHELXL-97 [7] were employed.

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**Table 1.** Structure data for trigonal B<sub>2</sub>O<sub>3</sub> form I as published by *Gurr et al.* in 1970 [1]

| hP15 (144) P3 <sub>1</sub> -a <sup>5</sup> $a = 4.3358(5) \text{ \AA}$ , $c = 8.3397(18) \text{ \AA}$ , $\gamma = 120^\circ$ |                  |            |            |             |                  |
|--|------------------|------------|------------|-------------|------------------|
| Atom   | Wyckoff position | $x$        | $y$        | $z$         | $B/\text{\AA}^2$ |
| B1   | 3a               | 0.2229(48) | 0.3926(47) | −0.0198(26) | 1.28(0.39)       |
| B2   | 3a               | 0.8281(43) | 0.6031(45) | 0.0921(24)  | 0.81(0.36)       |
| O1   | 3a               | 0.5468(30) | 0.3972(32) | 0.0000(00)  | 0.82(0.16)       |
| O2   | 3a               | 0.1485(21) | 0.6004(33) | 0.0775(09)  | 0.75(0.16)       |
| O3   | 3a               | 0.0045(24) | 0.1608(36) | −0.1291(23) | 0.58(0.12)       |

Isotropic displacement parameters were allowed to vary; the small amount of data does not allow to refine significant anisotropic displacement parameters for the atoms.

The results of structure refinements in the space groups P3<sub>1</sub> and P3<sub>1</sub>21 differ only insignificantly (Table 2). In any case, the enlargement of the number of refined parameters is not justified. The increase of the space group symmetry increases also the *Laue* symmetry from  $\bar{3}$  to  $\bar{3}m$ . For the latter, the volume of the asymmetric unit is only half as big, and in particular the *hkil* reflections must have now the same intensity as the *khil* reflections. In the data set of *Gurr et al.* [1] there are 18 such reflection pairs. The internal *R* value based on these reflections is 0.029 which supports our choice of the higher *Laue* symmetry. In addition, there are larger elements in the correlation matrix after refinement in P3<sub>1</sub>. More details on the refinement can be obtained from the data in CIF format which have been deposited at the Inorganic Crystal Structure Database at the Fachinformationszentrum Karlsruhe under the deposition number CSD 411992.

The new positional atom coordinates of trigonal B<sub>2</sub>O<sub>3</sub> form I described in space group (152) P3<sub>1</sub>21 can be found in Table 3. These data have been standardized with

**Table 2.** Comparison of structural refinements in space group P3<sub>1</sub> and P3<sub>1</sub>21

|  | P3 <sub>1</sub> | P3 <sub>1</sub> 21 |
|--|-----------------|--------------------|
| $R_1 = \Sigma(F_o - F_c)/\Sigma F_o$                                     | 0.052           | 0.052              |
| $wR_2 = (\Sigma w(F_o^2 - F_c^2)^2 / \Sigma (wF_o^2)^2)^{0.5}$ ; $w = 1$ | 0.121           | 0.122              |
| $Goof = (\Sigma (w(F_o^2 - F_c^2)^2) / (n - p))^{0.5}$                   | 0.675           | 0.703              |
| Number of free variables ( $p$ )   | 21              | 11                 |
| Number of reflections ( $n$ )  | 130             | 112                |
| Final difference <i>Fourier</i> map ( $\text{e\AA}^{-3}$ )               | −0.28 to +0.38  | −0.31 to +0.37     |

**Table 3.** New structure data for trigonal B<sub>2</sub>O<sub>3</sub> form I

| hP15 (152) P3 <sub>1</sub> 21-c <sup>2</sup> a $a = 4.3358 \text{ \AA}$ , $c = 8.3397 \text{ \AA}$ , $\gamma = 120^\circ$ |                  |            |            |           |                  |
|---|------------------|------------|------------|-----------|------------------|
| Atom  | Wyckoff position | $x$        | $y$        | $z$       | $U_{\text{iso}}$ |
| B   | 6c               | 0.3954(19) | 0.2299(23) | 0.2244(9) | 0.0102(14)       |
| O1  | 6c               | 0.6009(12) | 0.1477(10) | 0.1282(5) | 0.0101(11)       |
| O2  | 3a               | 0.1607(14) | 0          | 1/3       | 0.0092(14)       |

**Table 4.** Interatomic bond lengths (Å) and bond angles (°)

| Bond lengths      |          | Bond angles           |          |
|-------------------|----------|-----------------------|----------|
| B–O1 <sup>a</sup> | 1.375(9) | O1 <sup>a</sup> –B–O2 | 116.3(6) |
| B–O2              | 1.356(8) | O1 <sup>a</sup> –B–O1 | 120.4(6) |
| B–O1              | 1.373(8) | O2–B–O1               | 123.1(7) |
|                   |          | B–O1–B <sup>b</sup>   | 130.9(5) |
|                   |          | B–O2–B <sup>c</sup>   | 135.0(8) |

Symmetry codes other than  $x, y, z$ : <sup>a</sup>  $-x + 1, -x + y + 1, -z + 1/3$ ; <sup>b</sup>  $-x + 1, -x + y, -z + 1/3$ ;  
<sup>c</sup>  $x - y, -y, -z + 2/3$

the computer program STRUCTURE TIDY [8]. Selected bond lengths and angles are presented in Table 4.

The B atom is triangularly coordinated to O atoms. The BO<sub>3</sub> triangle is very close to planar, the sum of the three O–B–O angles being 359.8(6)°. The two crystallographically independent O atoms have site symmetry 1 and 2, respectively. They are coordinated to two B atoms each. The coordination figures are more regular than in the P3<sub>1</sub> structure. The new structure description is in accordance with results from NMR measurements which show that the B atoms are in a trigonal planar environment [9]. The absence of more than one distinguishable splitting suggests that all BO<sub>3</sub> groups in the normal pressure modification of B<sub>2</sub>O<sub>3</sub> are bonded in one configuration only. Contrary to the old structure proposal, the trigonal B<sub>2</sub>O<sub>3</sub>–I modification does not have a polar axis which allows to make some statements about selected physical properties as *e.g.* on pyroelectricity which cannot occur in this compound.

## References

- [1] Gurr GE, Montgomery PW, Knutson CD, Gorres BT (1970) Acta Cryst **B26**: 906
- [2] Prewitt CT, Shannon RD (1968) Acta Cryst **B24**: 869
- [3] Berger SV (1952) Acta Cryst **5**: 389
- [4] Berger SV (1953) Acta Chem Scand **7**: 611
- [5] Strong SL, Kaplow R (1968) Acta Cryst **B24**: 1032
- [6] Wilson AJC (ed) (1992) International Tables for Crystallography, vol C. Kluwer, Dordrecht
- [7] Sheldrick GM (1997) SHELXL-97, Program for Crystal Structure Refinement, Univ Göttingen, Germany
- [8] Gelato LM, Parthé E (1987) J Appl Cryst **20**: 139
- [9] Svanson SE, Forslind E, Krogh-Moe J (1962) J Phys Chem **66**: 174

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